## Limits \& Continuity

## 1.4 - Continuity

## Continuity from PreCalculus

A function is said to be continuous at $c$ if its graph passes through the point at $x=c$ without a "hole" or a"jump"





## Continuity from Calculus

A function $f$ is continuous at $c$ if the following three conditions hold:

1. $f(c)$ is defined
2. $\lim _{x \rightarrow c} f(x)$ exists
3. $\lim _{x \rightarrow c} f(x)=f(c)$
$f$ is discontinuous at $c$ if one or more of these conditions fails to be true.

## Which Functions Are Continuous?

If functions $f$ and $g$ are continuous at $c$, then the following are also continuous at $c$ :

1. $f \pm g$
2. $a \bullet f \quad[$ for any constant $a$ ]
3. $f \bullet g$
4. $f / g$
[if $g(c) \neq 0$ ]
5. $f(g(x)) \quad[$ for $f$ continuous at $g(c)]$

All polynomial functions are continuous. Rational functions are not continuous when the denominator $=$ 0 (vertical asymptote). Piece-wise functions have the potential to be continuous or not.

## Limits \& Continuity

## 1.4 - Continuity

Ex A: Determine if each function is continuous If discontinuous, state why.
\#1)

\#2)

\#3)


Ex B: Determine if each function is continuous. If discontinuous, state where it is discontinuous and why.
\#1) $\quad f(x)=x^{3}-3 x^{2}-x+3$
\#2) $\quad f(x)=\frac{1}{(x-1)^{2}}$
\#3) $\quad f(x)= \begin{cases}2 x+1 & \text { if } x<2 \\ -2 x+9 & \text { if } x \geq 2\end{cases}$
\#4) $\quad f(x)=\left\{\begin{array}{cc}x^{2}+1 & \text { if } x<4 \\ 5 x-1 & \text { if } x \geq 4\end{array}\right.$

