

# Derivative Applications

## Chapter 3 Review

### Dirty Inc's Looks

#1) Dirty Inc specializes in selling dirty looks to customers whose faces are too nice to be able to form their own dirty looks. Dirty Inc's profit function is  $P(x) = 20\sqrt{x} - 12\sqrt[3]{x}$  dollars, where  $x$  is the daily sales of dirty looks

- Find the marginal profit function.
- Find the marginal profit when 16 dirty looks have been sold.
- Interpret your answer from part b.

### Anti Inc's Jokes

#2) Anti Inc sells jokes by the punchline. Their top seller is

Question: "What is red, has large talons, whistles when you squeeze it, and likes to be called Reggie?"

Punchline: "A turtle.

So maybe I lied about it being red... and the talons.

Come to think of it, I lied about the whistling.

And tbh, his name isn't even Reggie.

Yeah, I guess I lied about the whole thing."

Anti Inc's revenue function is  $R(x) = 30\sqrt[3]{x} + 4\sqrt{x}$  dollars, where  $x$  is the daily sales of punchlines.

- Find the marginal revenue function.
- Find the marginal revenue when 32 punchlines have been sold.
- Interpret your answer from part b.

# Derivative Applications

## Chapter 3 Review

### Butt Munchers

#3) A growing problem among smokers is their tendency to litter. Scott's entrepreneurial spirit and scientific knowhow has led him to develop a new line of gerbil that will actually munch on the butts of cigarettes. The cigarette butt munchers have a cost of \$5.00 each with fixed costs \$1000 per week.

- a. Find the cost function.
- b. Find the average cost function.
- c. Find the marginal average cost function.
- d. Evaluate  $MAC(x)$  at  $x = 10$  and interpret your answer.

Find the first four derivatives of each function.

#4)  $f(x) = 2x^4 + x - 8$  (Use Leibniz)

#5)  $f(x) = \sqrt{x^3}$  (Use Newton)

## Derivative Applications

### Chapter 3 Review

#6) If  $f(x) = \frac{x^2+1}{2x}$ , find  $f''(3)$ .

#8) If  $f(x) = (5x^2 + 3x - 1)(x^2 + 1)$ , find the first and second derivative.

#7) If  $f(x) = \frac{x+1}{x-1}$ , find  $f''(3)$ .

#9) If  $f(x) = \frac{1}{x-1}$ , find the first and second derivative.

# Derivative Applications

## Chapter 3 Review

#10)  $\frac{d^2}{dr^2}(\pi r^2)|_{r=3}$

#11)  $\frac{d^2}{dr^2}(r^5 + r^4)|_{r=2}$

### Imagination Population

#12) The population of my imaginary friends  $t$  nervous breakdowns from now is predicted to be  $p(t) = 12t^{3/2} + 5$  people.

- Find  $p(2)$  and interpret your answer.
- Find  $p'(2)$  and interpret your answer.
- Find  $p''(2)$  and interpret your answer.

# Derivative Applications

## Chapter 3 Review

### Pizza Rolls

#13) The average time it takes for a  $350^\circ$  Pizza Roll to exit the oven and enter my waiting, salivating mouth is 2.3 seconds. A Pizza Roll's temperature  $t$  seconds after burning my tongue is  $T(t) = -10\sqrt{t} + 350$  degrees F.

- Find  $T(4)$  and interpret your answer.
- Find  $T'(4)$  and interpret your answer.
- Find  $T''(4)$  and interpret your answer.

### German Chocolate

#14) A delicious cake is dropped from a reverse albino pigeon while in flight. The height of the moist German chocolate cake after  $t$  seconds is  $s(t) = 75 - 16t^2$  feet (neglecting air resistance, obviously).

- How long will it take the German chocolate cake to reach the ground?
- What will the velocity of the cake be when it impacts the ground?

*The cake is a lie.*

# Derivative Applications

## Chapter 3 Review

### Cat-a-pterodactyl

#15) A evolutionary cat-a-pterodactyl (yes, it's exactly what you think it is) is carrying a newt. The cat-a-pterodactyl is planning on dropping the newt on an unsuspecting dog-a-saurus (also, what you think it is.) The newt will fall a distance of  $s(t) = 16t^2$  feet (neglecting all logic and reasoning, of course). Please note  $t$  is the time in seconds after the cat-a-pterodactyl's talons/paws let go of the flesh of the newt.

- If it takes 4 seconds to hit the dog-a-saurus, find the impact velocity.
- Find the acceleration due to gravity.

#16)  $P(x)$  = total profit from selling  $x$  blocks of head  
 $x$  = number of blocks of head

Interpret  $P(3) = \$21$

Interpret  $MP(3) = \$8$  (Give two interpretations)

Interpret  $AP(3) = \$7$

Interpret  $MAP(70) = \$1$