

## 1.2 Limits Analytically

Calculus

Name: \_\_\_\_\_

**Practice**

**Evaluate each limit.**

1. $\lim_{x \rightarrow 2} (x - x^2)$	2. $\lim_{x \rightarrow 5} (x + 1)^2$	3. $\lim_{x \rightarrow 1} \frac{x^2 - 5x}{x - 1}$	4. $\lim_{x \rightarrow 1} \frac{x^2 + x - 30}{x - 1}$
5. $\lim_{x \rightarrow 0} \frac{\sqrt{x+7} - \sqrt{7}}{x}$	6. $\lim_{x \rightarrow 7} \frac{\sqrt{x+9} - 4}{x - 7}$	7. $\lim_{x \rightarrow 0} \frac{3x}{\sin x}$	8. $\lim_{x \rightarrow 0} \frac{\sin(2x)}{3x}$
9. $\lim_{x \rightarrow -2} (3x^2 - x + 1)$	10. $\lim_{x \rightarrow 3} (2x^2 + 5x - 6)$	11. $\lim_{x \rightarrow -7} \frac{2x^3 + 11x^2 - 21x}{x^2 + 7x}$	12. $\lim_{x \rightarrow 8} \frac{x^2 + 2x - 80}{x - 8}$
13. $\lim_{x \rightarrow 0} \frac{\sqrt{x+9} - 3}{x}$	14. $\lim_{x \rightarrow 0} \frac{\sqrt{x+11} - \sqrt{11}}{x}$	15. $\lim_{x \rightarrow 5} \sqrt{4x - 9}$	16. $\lim_{x \rightarrow -1} \sqrt{3 - x}$
17. $\lim_{h \rightarrow 0} \frac{\frac{1}{x+h} - \frac{1}{x}}{h}$	18. $\lim_{h \rightarrow 0} \frac{5\sqrt{x+h} - 5\sqrt{x}}{h}$	19. $\lim_{x \rightarrow 0} \frac{\sin(5x)}{\sin(8x)}$	20. $\lim_{x \rightarrow 0} \frac{\sin(4x)}{\sin(2x)}$
21. $\lim_{x \rightarrow 1} 3$	22. $\lim_{x \rightarrow -3} 14$	23. $\lim_{x \rightarrow 2} \frac{\sqrt{5x-6}}{x}$	24. $\lim_{x \rightarrow \frac{\pi}{2}} \tan\left(\frac{x}{2}\right)$

25. $\lim_{x \rightarrow \frac{1}{3}} \frac{6x^2 + 13x - 5}{3x - 1}$	26. $\lim_{x \rightarrow 0} \frac{7x^2 + x}{x}$	27. $\lim_{x \rightarrow 0} \frac{\frac{1}{x+3} - \frac{1}{3}}{x}$	28. $\lim_{x \rightarrow 0} \frac{\frac{1}{(x+2)^2} - \frac{1}{4}}{x}$
29. $\lim_{x \rightarrow 0} \frac{\tan(6x)}{\sin(5x)}$	30. $\lim_{x \rightarrow 0} \frac{(1 - \cos^2 x) \sin x}{x^2}$	31. $\lim_{x \rightarrow 0} (-2)$	32. $\lim_{x \rightarrow 1} \frac{\sqrt{x+5} + \sqrt{6}}{x}$
33. $\lim_{x \rightarrow 0} \frac{x^2 + 2x - 8}{x - 4}$	34. $\lim_{x \rightarrow -2} \frac{x^2 - 4x - 10}{x}$	35. $\lim_{x \rightarrow 0} \frac{3x^2 + 5x}{x}$	36. $\lim_{x \rightarrow 4} \frac{5x^2 - 21x + 4}{x - 4}$
37. $\lim_{h \rightarrow 0} \frac{(x+h)^2 + 6(x+h) - (x^2 + 6x)}{h}$	38. $\lim_{h \rightarrow 0} \frac{4(x+h)^2 - 5(x+h) - 2 - (4x^2 - 5x - 2)}{h}$	39. $\lim_{x \rightarrow 0} \frac{\sin^2(7x)}{\sin^2(9x)}$	
40. $\lim_{x \rightarrow 0} \frac{5x}{\tan(4x)}$	41. $\lim_{x \rightarrow \frac{1}{2}} \frac{1 - x - 2x^2}{2x - 1}$	42. $\lim_{x \rightarrow \pi} \cos x$	43. $\lim_{x \rightarrow \frac{\pi}{8}} \sin(4x)$
44. $\lim_{x \rightarrow 2} \frac{x^2 + 6x - 16}{2 - x}$	45. $\lim_{x \rightarrow 5} \frac{2x^2 - 17x + 35}{5 - x}$	46. $\lim_{x \rightarrow 0} \frac{x \cot(5x)}{\cos(5x)}$	47. $\lim_{h \rightarrow 0} \frac{6 - 3(x+h) - (6 - 3x)}{h}$

Using the following piecewise functions, find the given values.

$g(x) = \begin{cases} \sqrt{5-x}, & x < -4 \\ x^2 - 5, & -4 \leq x < 2 \\ x - 3, & x \geq 2 \end{cases}$	$h(x) = \begin{cases} - x , & x \leq -5 \\ 20 - x^2, & -5 < x \leq 3 \\ 4x - 1, & x > 3 \end{cases}$	$w(\theta) = \begin{cases} \sin \theta, & \theta \leq \pi \\ \cos \theta, & \pi < \theta < 2\pi \\ \tan \theta, & \theta > 2\pi \end{cases}$
$\lim_{x \rightarrow 2^-} g(x) =$	$\lim_{x \rightarrow -5^+} h(x) =$	$\lim_{x \rightarrow \pi^-} w(\theta) =$
$\lim_{x \rightarrow -4^+} g(x) =$	$\lim_{x \rightarrow -5} h(x) =$	$w(\pi) =$
$g(2) =$	$h(3) =$	$\lim_{x \rightarrow \pi^+} w(\theta) =$
$\lim_{x \rightarrow -4^-} g(x) =$	$\lim_{x \rightarrow -5^-} h(x) =$	$\lim_{x \rightarrow 2\pi^-} w(\theta) =$
$\lim_{x \rightarrow 2^+} g(x) =$	$\lim_{x \rightarrow 3^+} h(x) =$	$\lim_{x \rightarrow \pi} w(\theta) =$
$\lim_{x \rightarrow 2} g(x) =$	$\lim_{x \rightarrow 3} h(x) =$	$\lim_{x \rightarrow 2\pi^+} w(\theta) =$
$\lim_{x \rightarrow -4} g(x) =$	$h(-5) =$	$\lim_{x \rightarrow 2\pi} w(\theta) =$
$g(-4) =$	$\lim_{x \rightarrow 3^-} h(x) =$	$w(2\pi) =$

## Test Prep

### 1.2 Limits Analytically

1.  $\lim_{x \rightarrow -1} \cos(\pi x) =$

- (A)  $\pi$       (B) 1      (C) 0      (D) -1      (E) The limit does not exist

2. If  $f(x) = \begin{cases} \ln 3x, & 0 < x \leq 3 \\ x \ln 3, & 3 < x \leq 4 \end{cases}$ , then  $\lim_{x \rightarrow 3} f(x)$  is

- (A)  $\ln 9$       (B)  $\ln 27$       (C)  $3 \ln 3$       (D)  $3 + \ln 3$       (E) nonexistent

3. Evaluate  $\lim_{x \rightarrow 1} \frac{\ln x}{3x}$  is

- (A) 0      (B)  $\frac{3}{e}$       (C)  $e$       (D) 3      (E) The limit does not exist.

4.  $\lim_{x \rightarrow 0} 4 \frac{\sin x \cos x - \sin x}{x^2}$  is

- (A) 2                      (B)  $\frac{40}{3}$                       (C)  $\infty$                       (D) 0                      (E) undefined

5.  $\lim_{x \rightarrow 0} \frac{\tan^3(2x)}{x^3} =$

- (A) -8                      (B) -2                      (C) 2                      (D) 8                      (E) The limit does not exist.

6.  $\lim_{x \rightarrow a} \frac{x^2 - 2ax + a^2}{x - a} =$

- (A)  $-\infty$                       (B)  $a$                       (C) 0                      (D)  $\infty$                       (E) The limit does not exist.

7. Let  $f(x) = \begin{cases} \frac{\sin x}{x}, & x \geq 0 \\ \cos x, & x < 0 \end{cases}$  Which of the following statements about  $f(x)$  is true?

I.  $\lim_{x \rightarrow 0^+} f(x) = 1$

II.  $\lim_{x \rightarrow 0^-} f(x) = 1$

III.  $\lim_{x \rightarrow 0} f(x) = 1$

- (A) None of these statements are true.                      (B) I only                      (C) II only                      (D) I and II only                      (E) I, II, and III

8.  $\lim_{x \rightarrow 0} \left( \frac{3x^2 + 5\cos x - 5}{2x} \right) =$

- (A) 0                      (B)  $\frac{5}{2}$                       (C) 3                      (D) 4                      (E) Does not exist

9. If  $f(x) = \begin{cases} \ln x & \text{for } 0 < x \leq 2 \\ x^2 \ln 2 & \text{for } 2 < x \leq 4, \end{cases}$  then  $\lim_{x \rightarrow 2} f(x)$  is

- (A)  $\ln 2$                       (B)  $\ln 8$                       (C)  $\ln 16$                       (D) 4                      (E) nonexistent